

# Wide-Angle Image Stitching Using Multi-Homography Warping

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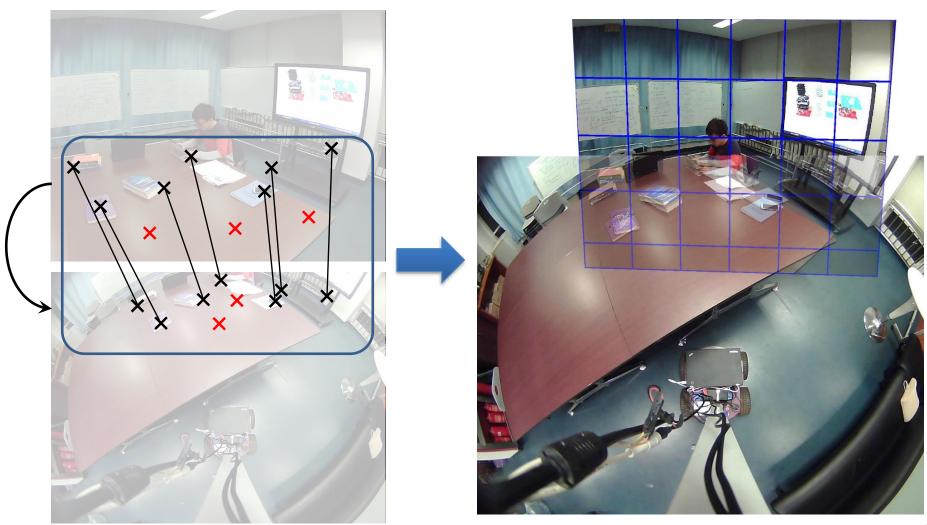
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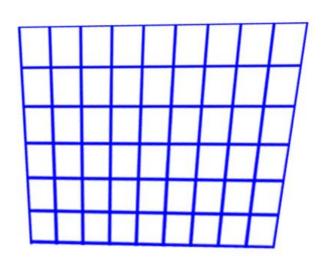
### Wide-angle image stitching





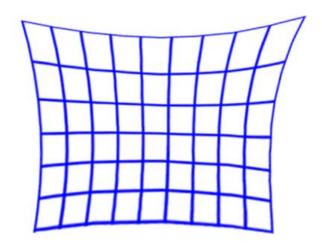
## Projective transformation (Homography)





Single global homography Misalignment

$$p' = H_g p$$



Division model
 Shape and area distortion

$$x' = x/(1+\lambda||x||^2)$$

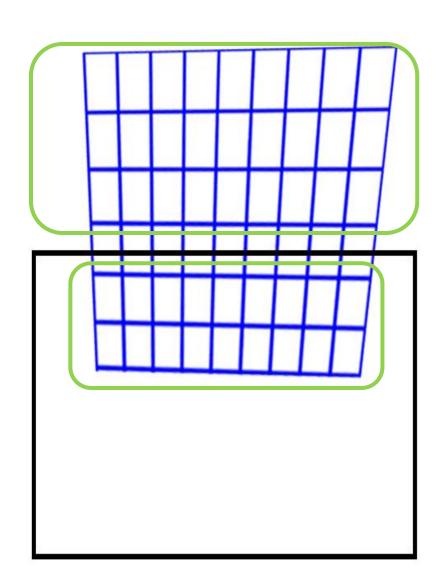
Globally similar
 (SPHP Warp, Chang' 14)
 (ANAP Warp, Lin' 15)

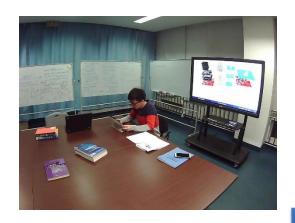


Locally aligned

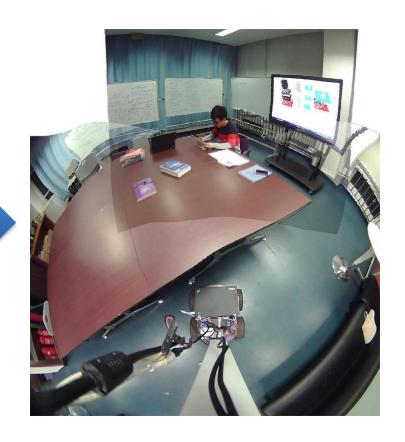
 (APAP Warp, Zaragoza' 13)
 (L-mDLT, Joo' 16)





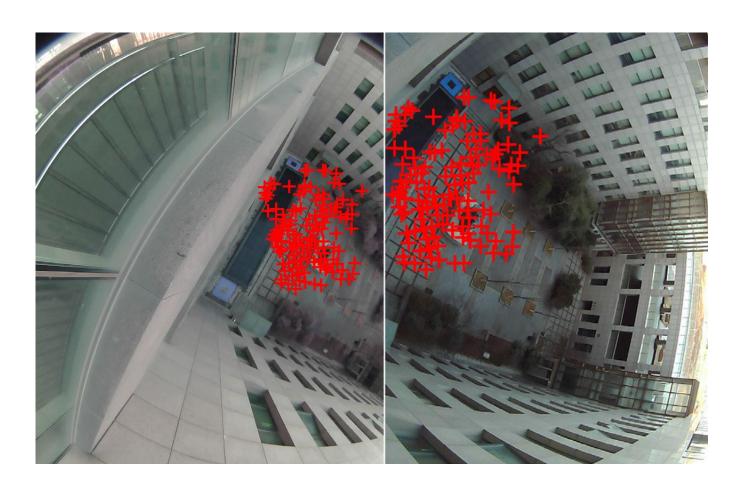






We propose a multi-homography warping, which integrates multiple local homographies with a global homography for accurate alignment and shape preservation.

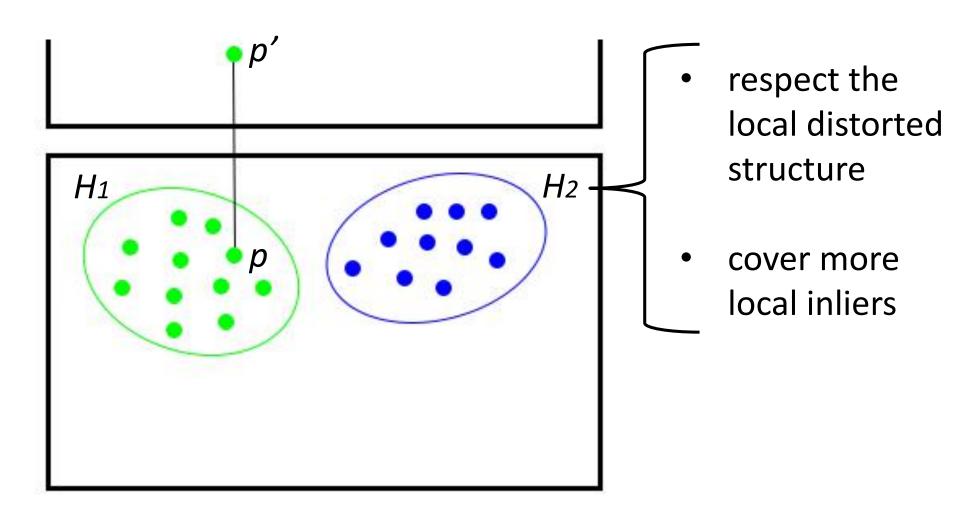
#### Inlier selection



Inliers selected by RANSAC (random sampling)



conditional sampling



**RANSAC**: homography hypotheses  $\{H_i\}_{i=1}^{M}$ 

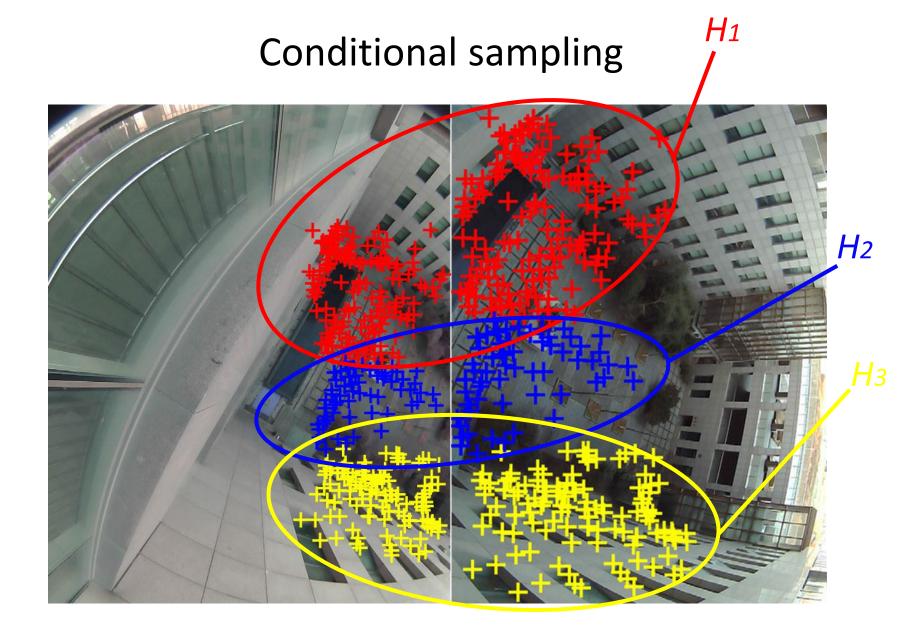
- Based on Multi-GS [Chin' 12], we use residual sorting information to perform a conditional sampling.
  - The probability of two points arising from the same homography can be encoded by residual sorting.
- For  $P_i = \{p_i, p_i'\}$  , we rank the  $\{H_i\}_{i=1}^M$  in terms of their residuals as

$$h^i = \{h_1, ..., h_M\}$$

• If  $P_i$  has been chosen, the probability of choosing  $P_i$  as the next sample is

$$f(P_i, P_j) = \frac{1}{a} |h_{1:a}^i \cap h_{1:a}^j|$$

- New hypotheses can be generated by using conditional sampling.
- We find the optimal hypothesis with the largest number of inliers to select the local inliers, and repeat the above procedure.



• Global homography  $H_{oldsymbol{g}}$ 

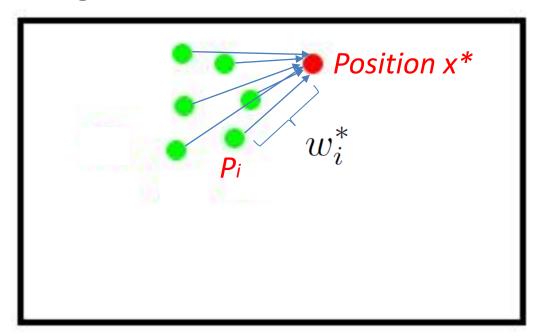
$$p' = H_g p$$
  $y' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 \\ h_7 & h_8 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$ 

Direct Linear Transformation (DLT)

$$0_{3\times 1} = ah = \begin{bmatrix} 0_{1\times 3} & -p^T & y'p^T \\ p^T & 0_{1\times 3} & -x'p^T \\ -y'p^T & x'p^T & 0_{1\times 3} \end{bmatrix} \begin{bmatrix} h_1 \\ \vdots \\ h_9 \end{bmatrix}$$

$$\hat{h} = \arg\min_{h} \sum_{i=1}^{n} ||a_i h||^2 = \arg\min_{h} ||Ah||^2$$

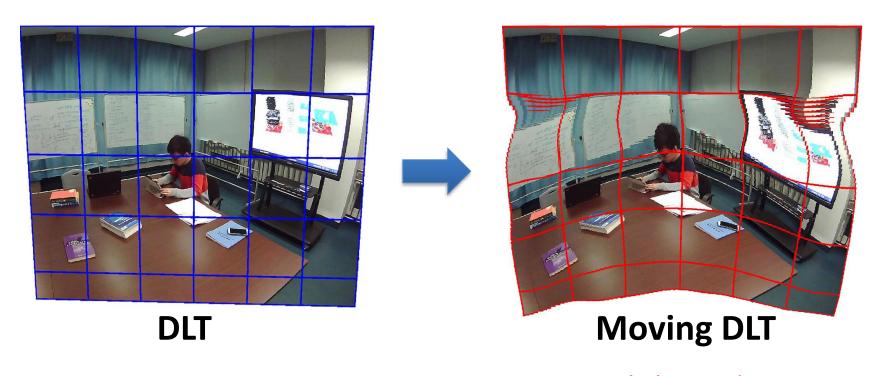
#### Moving DLT [Zaragoza' 13]



Local homographies  $h^*$ 

$$h^* = \arg\min_{h} \sum_{i=1}^{N} ||w_i^* a_i h||^2 = \arg\min_{h} ||W^* A h||^2$$

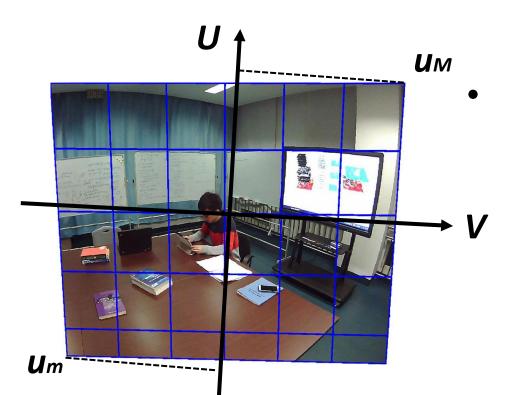
$$w_i^* = max(exp(-||x^* - p_i||^2/\sigma^2), \gamma)$$



Unnatural shape distortion

• We integrate the local  $\,h^*\,$  with global  $H_{g_*}$  as our *multi-homography warping* 

$$H_m^* = w_l^* h^* + (1 - w_l^*) H_g$$
$$w_l^* = (u^* - u_m) / (u_M - u_m)$$

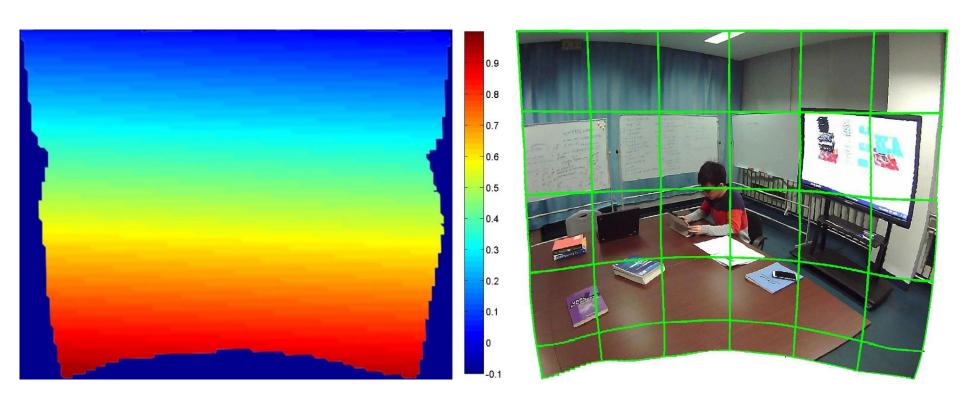


A rotation of the original coordinate system of the image warped by  ${\cal H}_a$ 

$$\theta = atan2(-h_8, -h_7)$$

$$(h_8, h_7 \text{ from } H_q)$$

#### Result

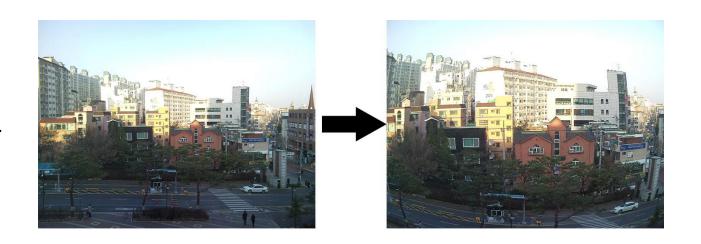


Weight map  $w_l^*$ 

$$H_m^* = w_l^* h^* + (1 - w_l^*) H_g$$

#### Two-view stitching

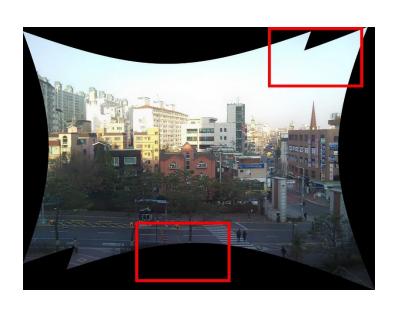
View 1



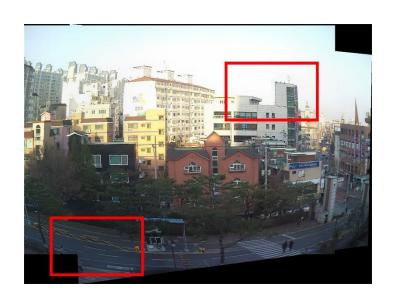
View 2



distortion factor  $\lambda = -0.4$  [Ju' 13]



Ju' 13



Stitching3pt













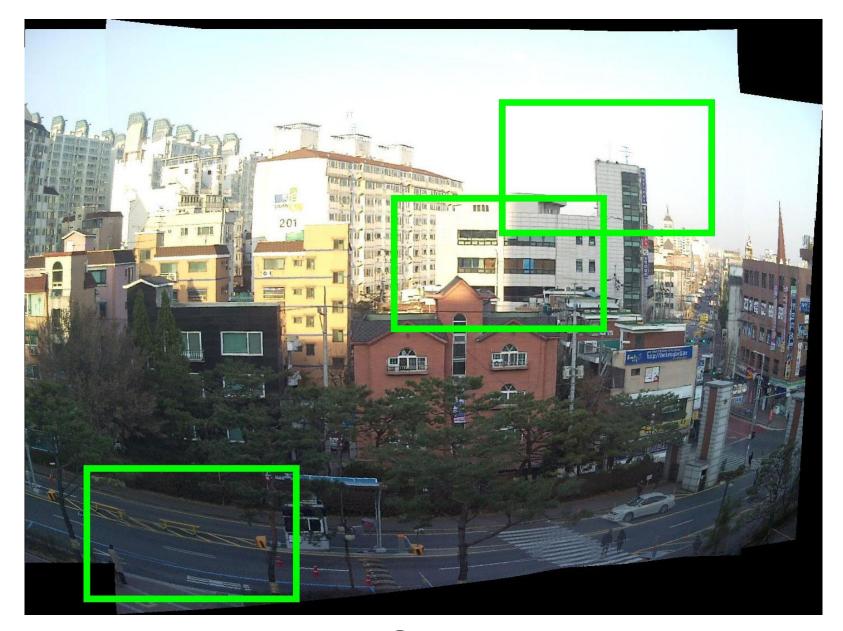
**Autostitch** 







**Microsoft ICE** 



Ours





Thank you!